UNIT-1

INTERFERENCE

Interference:

When two or more waves are superimposed then there is a modification of intensity or amplitude in the region of superposition. This modification of intensity or amplitude in the region of super position is called **Interference**.

When the resultant amplitude is the sum of the amplitudes due to two waves, the interference is known as **Constructive interference** and when the resultant amplitude is equal to the difference of two amplitudes, the interference is known as **destructive interference**.



PRINCIPLE OF SUPERPOSITION:

This principle states that the resultant displacement of particle in a medium acted upon by two or more waves simultaneously is the algebraic sum of displacements of the same particle due to individual waves in the absence of the others.

Consider two waves traveling simultaneously in a medium. At any point let y_1 be the displacement due to one wave and y_2 be the displacement of the other wave at the same instant.

Then the resultant displacement due to the presence of both the waves is given by

$$y = y_1 \pm y_2$$

+*ve* Sign has to be taken when both the displacements $y_1 \& y_2$ are in the same direction -*ve*Sign' has to be taken when both the displacements $y_1 \& y_2$ are in the opposite direction. **INTERFERENCE IN THIN FILMS**



Consider a thin film of thickness *t* and refractive index μ . A ray of light OA incident on the surface at an angle *i* is partly reflected along AB and partly refracted into medium along AC,

making an angle of refraction r .at C it is again partly reflected along CD. Similar refractions occur at E.

To find the path difference between the rays, draw DB perpendicular to AB Then the path difference = $\mu(AC + CD) - AB$(1) From triangle ACE CE

From triangle

From triangle

$$B = AD\cos(90 - i) = 2AE\sin i \quad \dots \dots \dots (4) \qquad (\therefore AD$$

FROM triangle ACE

$$\sin r = \frac{AE}{AC} \Rightarrow AE = AC \sin r$$
$$AE = \frac{t \sin r}{\cos r} \qquad (\quad \because AC = \frac{t}{\cos r})$$

From Eq (4)

$$AB = \frac{2t \sin r}{\cos r} \times \sin i$$

$$AB = \frac{2t \sin r \sin i}{\cos r} \times \frac{\sin r}{\sin r}$$

$$AB = \frac{2\mu t \sin^2 r}{\cos r} \qquad (\because \mu = \frac{\sin i}{\sin r})$$

$$(\because \mu = \frac{\sin i}{\sin r})$$

On substituting the values of AC, CD & AB from Eq(2),(3)&(5) in Eq(1), we get

The path difference =
$$\mu(\frac{t}{\cos r} + \frac{t}{\cos r}) - \frac{2\mu t \sin^2 r}{\cos r}$$

= $\frac{2\mu t}{\cos r}(1 - \sin^2 r) = \frac{2\mu t \cos^2 r}{\cos r} = 2\mu t \cos r$
 \therefore The path difference = $2\mu t \cos r$

According to the theory of reversibility, when the light ray reflected at rarer-denser interface, it introduces an extra phase difference π (or) path difference of $\frac{\lambda}{2}$ 2

> \therefore The actual path difference = $2\mu t \cos r - \frac{\lambda}{2}$ 2

Case.1: condition for maximum intensity

We know that the intensity is maximum when path difference= $n\lambda$

$$\therefore \text{ From Eq.(6) } 2\mu t \cos r - \frac{\lambda}{2} = n\lambda$$

$$2$$

$$2 \mu t \cos r = (2n + 1)\frac{\lambda}{2}$$

Case.2: condition for minimum intensity

We know that the intensity is minimum when path difference = $(2n+1)^{\frac{\lambda}{2}}$

$$\therefore \text{ from Eq.(6)} \quad 2\mu t \cos r - \frac{\lambda}{2} = (2n+1)\frac{\lambda}{2}$$
$$2\mu t \cos r = (n+1)\lambda$$

NEWTON'S RING EXPERIMENT

A Plano convex lens(L) having large focal length is placed with its convex surface on the glass plate(G₂).a gradually increasing air film will be formed between the plane glass plate and convex surface of Plano convex lens. The thickness of the air film will be zero at the point of contact and symmetrically increases as we go radially from the point of contact.

A monochromatic light of wavelength ' λ ' is allowed to fall normally on the lens with the help of glass plate (G₁) kept at 45⁰ to the incident monochromatic beam. A part of the incident light rays are reflected up at the convex surface of the lens and the remaining light is transmitted through the air film. Again a part of this transmitted light is reflected at on the top surface of the glass plate (G₁).both the reflected rays combine to produce an interference pattern in the form of alternate bright and dark concentric circular rings, known as Newton rings. The rings are circular because the air film has circular symmetry. These rings can be seen through the travelling microscope.



THEORY

Consider a Plano convex lens is placed on a glass plate. Let R be the radius of curvature and r be the radius of NEWTON ring, corresponding to constant film thickness.

As one of the rays suffers reflection at denser medium, so a further phase changes of π or path difference of $\frac{\lambda}{2}$ takes place.

The path difference between the rays =2 μ t cos r + $\frac{\lambda}{2}$ ------ (i)

For air $\mu = 1$, and normal incidence r = 0

 \therefore Path difference = $2t + \frac{\lambda}{2}$



AT THE POINT OF CONTACT

The thickness of the air film t=0, μ =1 & for normal incidence r = 0.

Then the path difference =
$$\frac{\lambda}{2}$$
.

If the Then the path difference = $\frac{\lambda}{2}$ then the corresponding phase difference is π .so that gives a dark spot is formed at the centre.

For bright ring

$$2t + \frac{\lambda}{2} = n\lambda$$
$$2t = (2n-1)\frac{\lambda}{2}$$
(ii)

For Dark ring

$$2t + \frac{\lambda}{2} = (2n+1)\frac{\lambda}{2}$$
$$2t = n\lambda$$
(iii)

In the above fig, from the property of the circle

$$NP \times NQ = NO \times ND$$

 $r \times r = 2t \times (2R - t)$
 $r^{2} = 2Rt - t^{2}$

As t is small, t^2 is very small. So t^2 is neglected.

$$\therefore r^{2} = 2Rt$$

$$t = \frac{r^{2}}{2R} \implies t = \frac{D^{2}}{8R}$$
(iv)

Thus for bright ring

 $_$ From Eq (ii) & (iv)

$$\frac{2D^2}{8R} = (2n-1)\frac{\lambda}{2}$$

$$D_n^2 = 2(2n-1)\lambda R \qquad (v)$$

Thus for dark ring

From Eq. (iii) & (iv)

$$\frac{2D^2}{8R} = n\lambda$$

$$D_n^2 = 4Rn\lambda \dots (vi)$$

$$D_n^2 = 4Rn\lambda$$

Determination of wave length of monochromatic light

From Eq(vi)
$$D_n^2 = 4Rn\lambda$$

For $n = m$, $D_m^2 = 4Rm\lambda$
 $\therefore D_m^2 - D_n^2 = 4Rm\lambda - 4Rn\lambda = 4R\lambda (m - n)$
 $\therefore \lambda = \frac{D_m^2 - D_n^2}{4R(m - n)}$ (vii)

This is the expression for wave length of monochromatic light.

Determination of refractive index of a liquid

The experimental set up as shown in fig. is used to find the refractive index of a liquid.

To find the refractive index of a liquid, the plane glass plate and Plano convex lens set up is placed in a small metal container. The diameter of nth and mth dark rings are determined, when there is air between Plano convex lens and plane glass plate.

Then we have,

$$D_m^2 - D_n^2 = 4Rm\lambda - 4Rn\lambda$$
$$= 4R\lambda(m-n) .$$

Now the given liquid whose refractive index (μ) is to be introduced in to the space between Plano convex lens and plane glass plate without disturbing the experimental set up.

Then the diameters of Newton's rings are changed. Now the diameter of nth and mth dark rings are measured.

Then $D_m^2 - D_n^2 = 4R\lambda (m-n)/\mu$ ------ (viii)

Therefore from (vii) & (viii) $\mu = \underline{D}_{\underline{m}}^2 - \underline{D}_{\underline{n}}^2$

CONDITIONS TO GET STATIONARY INTERFERENCE FRINGES

1. The two sources should be coherent.

- 2. The two sources must emit continuous waves of the same wavelength and same frequency.
- 3. The distance between the two sources (d) should be small.
- 4. The distance between the sources and the screen (D) should be large.
- 5. To view interference fringes, the back ground should be dark.
- 6. The amplitude of interfering waves should be equal.
- 7. The sources must be narrow, i.e., they must be extremely small.
- 8. The source must be monochromatic source.

Production of Colors in thin films:

With monochromatic light alternate dark and bright interference fringes are obtained.

With white light, the fringes obtained are colored. it is because the path difference $2\mu t \cos r - \frac{\lambda}{2}$

depends upon μ , *t* & *r*

- (i) Even if t and r kept constant, the path difference will change with $\mu \& \lambda$ of light used. White light composed of various colors from violet to red. The path difference also changes due to reflection at denser medium by $\frac{\lambda}{2} \operatorname{as} \lambda_{V} \langle \lambda_{R} \rangle$.
- (ii) If the thickness of the film varies with uniformly, if at beginning it is thin, which will appear black. as path difference varies with thickness of the film, it appears different colors with white light.
- (iii) If the angle of incidence changes, the angle of refraction is also changes, so that with white light, the film appears various colors when viewed from different directions.

DIFFRACTION

"When light is incident on the obstacles or small apertures whose size is comparable to wavelength of light, then there is a departure from straight line propagation, the light bends round the corners of the obstacles and enters into geometrical shadow. This bending of light is called diffraction."



Differences between Interference and diffraction

INTERFERENCE	DIFFRACTION
1. Superposition is due to two separate wave fronts originating from two coherent sources.	1. Superposition is due to secondary wavelets originating from different parts of same wave front.
2. Interference fringes may or may not be of same width.	2. Diffraction fringes are not of the same width
3. Points of minimum intensity are perfectly dark	3. Points of minimum intensity are not perfectly dark.
4. All bright bands are of uniform intensity	4. All bright bands are not of same intensity.

There are two types of Diffractions are there, they are

1. Fresnel Diffraction

2. Fraunhofer Diffraction

Fresnel diffraction

Fraunhofer diffraction



Differences between Fresnel Diffraction and Fraunhofer Diffraction

Fresnel Diffraction	Fraunhofer Diffraction
1. Eighter a point source or an illuminated narrow slit is used.	1. Extended source at infinite distance is used.
2. The wave front undergoing diffraction is either spherical or cylindrical.	2. The wave front undergoing diffraction is plane wave front.
3. The source and screen are at finite distances from the obstacle.	3. The source and screen are at infinite distances from the obstacle.
4. No lens is used to focus the rays.	4. Converging lens is used to focus the rays.

FRAUNHOFER DIFFRACTION AT SINGLE SLIT:



Consider a slit AB of width "e" and a plane wave front WW^1 of monochromatic light of wavelength " λ " is incident normally on the slit. The diffracted light through the slit is focused with the help of a convex lens on a screen. The screen is placed at the focal plane of the lens. Here the secondary wave lets spared out to the right in all directions.

 $\label{eq:constraint} The waves travelling along OP_o are brought out to focus at P_o by the lens. Hens P_O is the bright central image.$

The secondary wavelets at angle " θ " with normal are focused at P₁ on the screen. Depending upon path difference, P₁onmay be of maximum (or) minimum intensity point.

To find intensity at P_1 we drawn a normal AC from A to the light ray at B the path difference between the wave lets from A and B in the direction " θ " is given by

From TraingleABC, $\sin\theta = \frac{BC}{AB} \Rightarrow BC = AB\sin\theta = e\sin\theta$

 \therefore Phase difference $=\frac{2\pi}{\lambda}e\sin\theta$

Let us consider the width of the slit is divided into 'n' equal parts. Then the phase difference between any two consecutive waves from these parts would be.

$$\frac{1}{\pi} (total. phase) = \lim_{n \to \infty} \frac{2\pi}{\lambda} ...e \sin\theta = d \quad (say)$$

$$\therefore \text{ Resultant amplitude } R = \frac{a \sin \frac{nd}{2}}{\sin \frac{nd}{2}}$$

$$a \sin \left[\frac{n}{2} \times \frac{2\pi}{n\lambda} ...e \sin\theta \right] = \frac{a \sin \frac{nd}{2}}{2}$$

$$\therefore R = \frac{a \sin \left[\frac{n}{2} \times \frac{2\pi}{n\lambda} ...e \sin\theta \right]}{2n\lambda} ...e \sin\theta = \frac{1}{2}$$

$$= \frac{a \sin \left[\frac{n}{2} \times \frac{2\pi}{n\lambda} ...e \sin\theta \right]}{\sin \left[\frac{\pi e \sin\theta}{\lambda} \right]}$$

$$= \frac{a \sin \left[\frac{\pi e \sin\theta}{\lambda} \right]}{\sin \left[\frac{\pi e \sin\theta}{n\lambda} \right]}$$

$$\text{Let}\alpha = \frac{\pi e \sin\theta}{\lambda} . \text{ Then}$$

$$R = \frac{a \sin \alpha}{\sin \frac{\alpha}{n}} ...n$$

$$R = \frac{a \sin \alpha}{n}$$

$$R = \frac{a \sin \alpha}{n} = na \frac{\sin \alpha}{\alpha}$$
Now the intensity
$$I = R^2 = A^2 \left[\frac{\sin \alpha}{\alpha} \right]^2(1)$$

Principal Maximum:

$$R = A \frac{\sin \alpha}{\alpha} = \frac{A}{\alpha} \alpha - \frac{\alpha^{3}}{3!} + \frac{\alpha^{5}}{5!} - \frac{\alpha^{7}}{7!} + \dots$$

$$= A \left[1 - \frac{\alpha^{2}}{3!} + \frac{\alpha^{4}}{5!} - \frac{\alpha^{6}}{7!} + \dots \right]$$

The value of R will be maximum, when $\alpha = 0$, i.e. $\frac{\pi e \sin \theta}{\lambda} = 0$ or $\sin \theta = 0$

Or $\theta = 0$

 \therefore Maximum intensity I=R² =A², this is occurred at $\theta = 0$, this maximum is known as principal maximum.

Minimum intensity Positions:

The intensity will be minimum, when sin $\alpha=0$.

$$\therefore \alpha = \pm \pi, \pm 2\pi, \pm 3\pi, \dots, \pm m\pi$$
$$\alpha = \pm m\pi$$
$$\frac{\pi e \sin \theta}{\lambda} = \pm m\pi$$
$$e \sin \theta = \pm m\lambda$$

In this way, we obtain the points of min. inf. on either side of the principle maxima.

Secondary maxima:

In addition to principle maxima at α =0. There are weak secondary maxima between equally spaced minima. The points of secondary maxima obtained as follows.

$$I = A^{2} \prod_{\alpha} \frac{\sin \alpha}{\alpha} \prod_{\alpha} \frac{1}{\alpha}$$
$$\frac{dI}{d\alpha} = A^{2} \cdot 2 \frac{\sin \alpha}{\alpha} \frac{\alpha}{\alpha} \frac{\cos \alpha - \sin \alpha}{\alpha^{2}} = 0$$

0

From above either sin $\alpha=0$, or $\alpha \cos \alpha$ -sin $\alpha=0$ if sin $\alpha=0$, it is min. intensity position. Hence positions of maximum are obtained by

$$\alpha \cos \alpha - \sin \alpha =$$

 $\alpha \cos \alpha = \sin \alpha$

The values of α satisfying the above equation are obtained graphically by plotting curves $y = \alpha$, $y = \tan \alpha$ on the same graph. The points of intersection of two curves give the values of α which satisfy the equation (2)



From fig The points of intersections are $\alpha = 0, \pm 3\frac{\pi}{2}, \pm 5\frac{\pi}{2}, \dots, \alpha$ at these points we get secondary

maxima

Intensity distribution graph



Let A B and CD be two parallel slits of equal width '*e*' separated by an opaque distance *d*. The distance between the corresponding middle points of the two slits is (e + d). Let a parallel beam of monochromatic beam of wave length λ be incident normally upon to the two slits.

When a wave front is incident normally on both slits all the points with in the slits become the sources of secondary wavelets. The secondary waves traveling in the direction of incident light come to focus at P_0 while the secondary waves traveling in the direction making an angle with θ the incident light come to focus at P_1 .

According to the theory of diffraction at a single slit. The amplitude R due to all the wavelets diffracted from each slit in a dissection θ is given by.

$$R = A \frac{\sin \alpha}{\alpha}$$
 where $\alpha = \frac{\pi e \sin \theta}{\lambda}$

Thus for simplicity we can take two slits as equivalent to two sources S_1 and S_2 placed at mid points of the slits and each slit sending a wavelet of amplitude $\frac{A \sin \alpha}{\alpha}$ in the direction θ .

 $\therefore \text{ Resultant amplitude at a point P}_1 \text{ on the screen will be a result of interference between two waves of amplitude } \frac{A \sin \alpha}{\alpha} \text{ and having a phase difference.}$

The path difference between the wavelets from S_1 and S_2 in the dissection $\theta = S_2 k$.

$$\therefore phase.difference(\delta) = \frac{2\pi}{\lambda}(e+d)\sin\theta$$

1 1.00

Discussion of Intensity:

From equation (3) the resultant intensity depending upon the following two factors.

1. A^2 Which is same as the intensity in the case of single slit diffraction thus it gives α^2 intensity distribution in the diffraction pattern.

2. $\cos^2 \beta$ Which gives the intensity pattern due to two waves interfere.

The resultant intensity at any point on the screen is given by the product of these two factors.

 \therefore Diffraction term $\frac{\sin^2 \alpha}{\alpha^2}$ gives the (i) Central maximum at $\theta = 0$

(ii) Minimum intensity positions $\alpha = \pm m\pi$

$$\frac{\pi e \sin \theta}{\lambda} = \pm m\pi$$
$$e \sin \theta = \pm m\lambda$$

(iii)

.Secondary maxima obtained at $\alpha = \pm 3\frac{\pi}{2}, \pm 5\frac{\pi}{2}, \dots$

On taking these three points plotted as graph as shown in the fig(a).

The interference term $\cos^2\beta$ gives the maximum

$$\cos^{2} \beta = 1 \Rightarrow \beta = \pm m\pi$$
$$\frac{\pi}{\lambda} (e+d)\sin\theta = \pm m\pi$$
$$(e+d)\sin\theta = \pm m\lambda$$

This is plot as shown in fig.(b)

The resultant intensity graph is as shown in fig. (c)



Diffraction at N-Parallel slits [Diffraction grating]



An arrangement consists of large no. of parallel slits of same width and separated by equal

opaque spaces is known as diffraction grating.

If there are N slits.

The path difference between any two consecutive slits is $= (e+d)\sin\theta$

$$\therefore \text{ Phase difference} = \frac{2\pi}{\lambda} (e+d) \sin\theta = 2\beta$$

By the method of vector addition of amplitudes

$$R = \frac{a \sin \frac{nd}{2}}{\sin \frac{d}{2}}$$

In this case $a = \frac{A \sin \alpha}{\alpha}$, $n = N$ and $d = 2\beta$
 $\therefore R = \frac{A \sin \alpha}{\alpha} \cdot \frac{\sin N\beta}{\sin \beta}$
 $I = R^2 = \begin{bmatrix} A \sin \alpha \|^2 \sin \beta \| \sin N\beta \|^2}{\frac{\alpha}{\beta} \| \frac{\beta}{\beta} \| \frac{$

Principle maxima:

The intensity will be maximum when $\sin \beta = 0$

$$\beta = \pm n\pi, n = 0, 1, 2, 3, \dots$$

But at the same time Sin N $\beta = 0$. So that the factor $\begin{bmatrix} \sin N\beta & 0 \\ -\sin \beta & 0 \end{bmatrix}$ becomes indeterminate.

$$\therefore \lim_{\beta \to n\pi} \frac{\sin N\beta}{\sin \beta} = \lim_{\beta \to n\pi} \frac{N \cos N\beta}{\cos \beta} = \pm N$$
$$\lim_{\beta \to n\Pi} \left\| \frac{\sin N\beta}{\sin \beta} \right\|_{\beta \to n\Pi}^{2} = N^{2}$$
$$\therefore \text{ The Resultant intensity } I = \left\| \frac{A \sin \alpha}{\alpha} \right\|_{\beta \to n\Pi}^{2}$$

i.e. The principle maxima obtained for $\beta = \pm n\pi$

$$\frac{\pi (e+d)\sin\theta}{\lambda} = \pm n\pi$$
$$(e+d)\sin\theta = \pm n\lambda$$

Minimum Intensity Positions:

Intensity I is the minimum when $\sin N\beta = 0$, but $\sin \beta \neq 0$

$$\therefore N\beta = \pm \pi, \pm 2\pi, \pm 3\pi, \dots$$
$$\frac{N\pi (e+d)\sin\theta}{\lambda} = \pm m\pi$$
$$N(e+d)\sin\theta = \pm m\lambda$$

Where m having all values except

 $0, N, 2N, \dots, nN.$ *i.e.* $m = 1, 2, \dots, (N - 1), (N + 1), \dots, (2N - 1), (2N + 1), \dots, (2N$ Secondary maximum: I maximum when $\frac{dI}{d\beta} = 0$ $\frac{d}{d\beta} \left[(A \frac{\sin \alpha}{\alpha})^2 (\frac{\sin N\beta}{\sin \beta})^2 \right] = 0$ $\left(\frac{A\sin\alpha}{\alpha}\right)^{2} 2\left[\frac{\sin N\beta}{\beta}\right] \left[\frac{N\sin\beta\cos N\beta - \sin N\beta\cos\beta}{\sin^{2}\beta}\right] = 0$ $N\sin\beta\cos N\beta - \sin N\beta\cos\beta = 0$ $N\sin\beta\cos N\beta = \sin N\beta\cos\beta$ $N\sin\beta = \cos\beta(\frac{\sin N\beta}{2})$ $\cos N\beta$ $\tan N\beta = \frac{N}{\cot \beta}$ JN2+00 N Nβ cot B $\therefore \sin N\beta = \frac{N}{\sqrt{(N^2 + \cot^2 \beta)}}$ $\frac{\sin^2 N\beta}{\sin^2 \beta} = \frac{N^2}{(N^2 + \cot^2 \beta) \sin^2 \beta}$ $=\frac{N^2}{N^2\sin^2\beta+\cos^2\beta}$ $=\frac{N^2}{N^2\sin^2\beta+1-\sin^2\beta}$ $\therefore \frac{\sin^2 N\beta}{\sin^2 \beta} = \frac{N^2}{1 + (N^2 - 1)\sin^2 \beta}$ $I_{\rm sec} = (A \frac{\sin \alpha}{\alpha})^2 \left[\frac{N^2}{(N^2 - 1)\sin^2 \beta} + 1\right]$

 $\therefore \frac{\text{int ensity.of.sec.ondary max ima}}{\text{int ensity.of.principle max ima}}$ $= \frac{N^2}{(1+(N^2-1)\sin^2\beta) \times N^2}$ $\therefore \frac{\text{int ensity.of.sec.ondary max ima}}{\text{int ensity.of.principle max ima}} = \frac{1}{1+(N^2-1)\sin^2\beta}$

From this we conclude that as the value of N increases the intensity of secondary maxima will decreases



GRATING SPECTRA



We know that the principle maxima in a grating are formed in a direction θ is given by $(e+d)\sin\theta = \pm n\lambda$

Where (e + d) grating element is θ is the angle diffraction and λ is Wave length

From the above equation, we conclude that

- 1. For a particular wave length λ , the angle of diffraction θ is different for different orders.
- 2. For white light and for an order *n* the light of different wave lengths will be diffracted in different directions. The longer the wavelength, greater is the angle of diffraction. So violet color being in the innermost position and red color in the outermost position.
- 3. Most of the intensity goes to zero order and rest is distributed among other orders thus the spectra become fainter as we go to higher orders.

Characteristics of grating spectra

- 1. Spectrum of different orders are situated symmetrically on both sides of zero order
- 2. Spectral lines are almost straight and quite sharp.
- 3. Spectral colors are in the order from violet to red.
- 4. Most of the intensity goes to zero order and rest is distributed among the other orders.

Maximum no. orders available with a grating

The principle maxima in grating satisfying the condition

$$(e+d)\sin\theta = n\lambda$$
$$n = \frac{(e+d)\sin\theta}{\lambda}$$
$$n_{\max} = \frac{(e+d)\sin 90^{0}}{\lambda}$$
$$n_{\max} = \frac{(e+d)}{\lambda}$$

DISPERSIVE POWER OF GRATING:

The dispersive power of grating is defined as the rate of variation of angle of diffraction with wavelength i.e., $\frac{d\theta}{d\lambda}$ is known as dispersive power of grating.

The condition for maxima is (e +d) $\sin \theta = n\lambda$

On differentiation we get (e+d) $\cos\theta \ d\theta = n \ d\lambda$



This is the expression for dispersive power of grating. **Conclusions :**

- > The dispersive power is directly proportional to diffraction order n.
- > The dispersive power is inversely proportional to grating element (e+d).
- > The dispersive power is inversely proportional to $\cos\theta$.

RESOLVING POWER OF GRATING:

The resolving power of a grating is defined as the capacity to form separate diffraction maxima of two wave lengths which are very close to each other



Let A B be a plane grating having grating element (e + d) and N be the total no. of slits. let a beam of wavelengths λ and $\lambda + d\lambda$ is normally incident on the grating in the fig P_1 is the n_{th} primary maximum of wavelength λ at an angle of diffraction θ_n and P_2 is the n_{th} primary maximum of wavelength $\lambda + d\lambda$ at an angle of diffraction $(\theta_n + d\theta_n)$.

According to Rayleigh's criterion, the two wave lengths will be resolved if the principle maximum of one falls on the first minimum of the other.

The principle maximum of λ in the direction θ_n is given by

$$(e+d)\sin\theta_n = \pm n\lambda$$
(1)

The wave length $(\lambda + d\lambda)$ form its n_{th} primary maxima in the direction $(\theta_n + d\theta_n)$

 $(e+d)\sin(\theta_n + d\theta_n) = \pm n(\lambda + d\lambda)$(2)

The first minimum of wave length λ from in the direction $(\theta_n + d\theta_n)$

$$N(e+d)\sin(\theta_n + d\theta_n) = (nN+1)\lambda$$
.....(3)

Multiplying eq(2) with N

$$N(e+d)\sin(\theta_n + d\theta_n) = \pm nN(\lambda + d\lambda)\dots(4)$$

From (3) & (4)

$$Nn(\lambda + d\lambda) = (nN + 1)\lambda$$
$$nN\lambda + nNd\lambda = nN\lambda + \lambda$$
$$nNd\lambda = \lambda$$
$$\frac{\lambda}{d\lambda} = nN$$

But from eq (1) $n = \frac{(e+d)\sin\theta_n}{\lambda}$ \therefore Re solving, power.of grating

$$\frac{\lambda}{d\lambda} = \frac{N(e+d)\sin\theta_n}{\lambda}$$

PREVIOUS OUESTIONS

- 1. What is meant by diffraction of light? Explain on the basis of Huygens wave theory.
- 2. Explain with necessary theory, the Fraunhofer diffraction due to 'n' slits.

(Or)

Give the theory of plane diffraction grating. Obtain the condition for the formation of nth order maximum.

3. Distinguish between Interference and Diffraction.

(Or)

How is diffraction different from Interference?

- 4. Calculate the maximum number of orders possible for plane diffraction grating.
- 5. Write notes on Rayleigh's criterion.
- 6. Distinguish between Fresnel and Fraunhoffer diffractions.
- 7. Define Resolving power of grating. Derive the expression for Resolving power of a grating based on Rayleigh's criterion.
- 8. Describe the action of plane transmission grating in producing diffraction spectrum.
- 9. Show that grating with 500lines/cm cannot give a spectrum in 4th order for the light of wave length 5890 A⁰.